

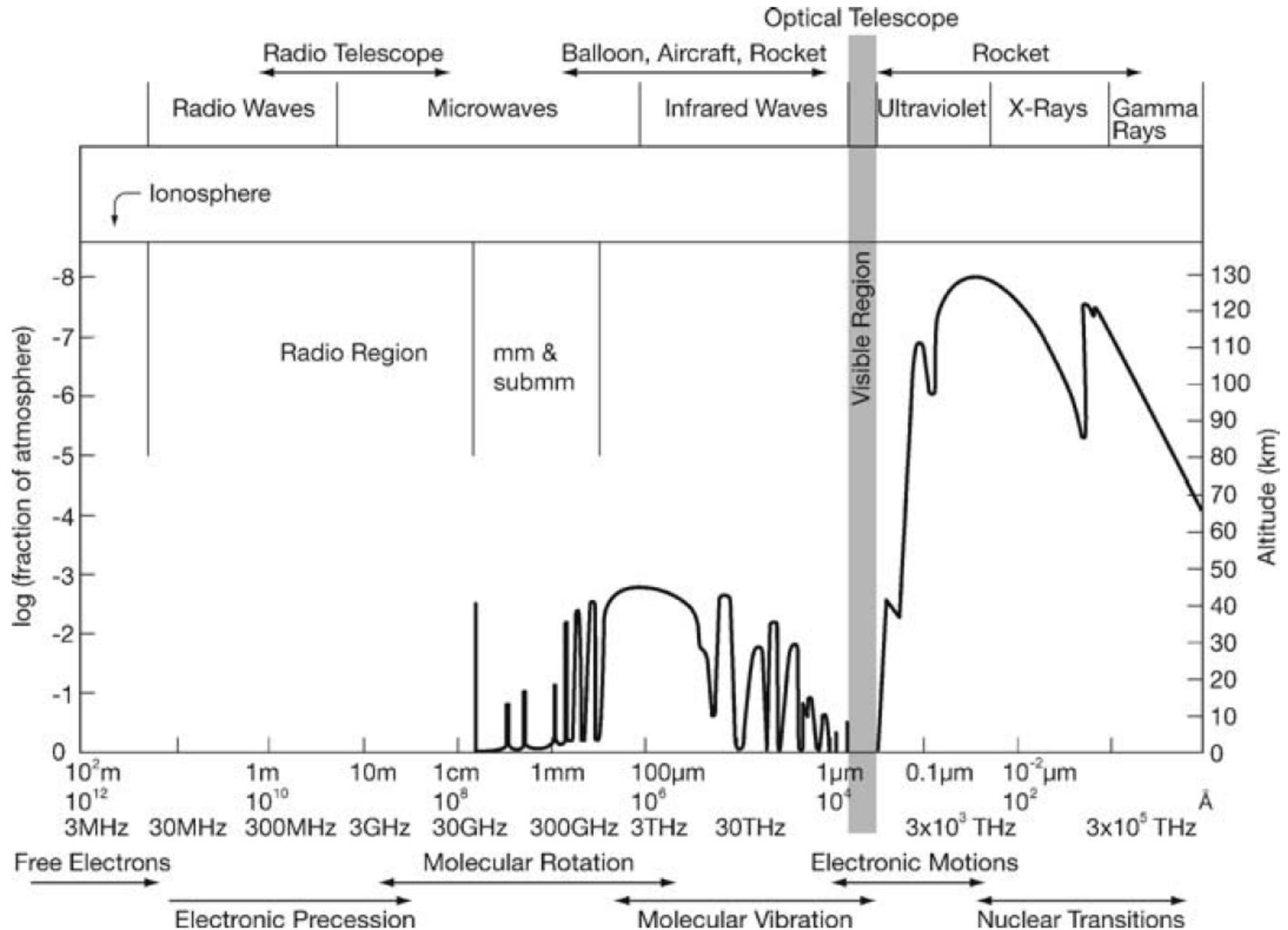
- Single dish radio telescopes

Astronomical Techniques II : **Lecture 2**

Ruta Kale

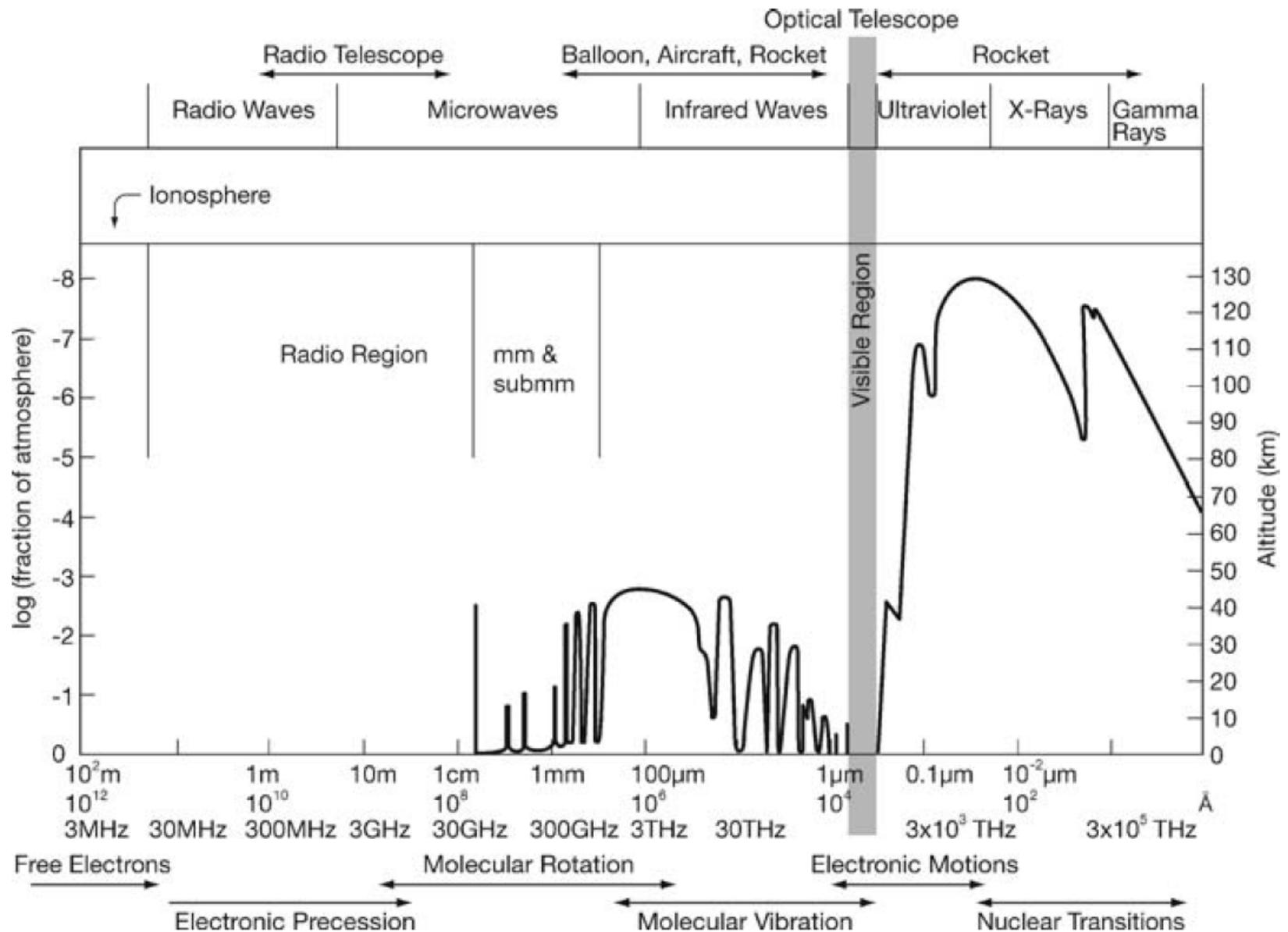
Essential Radio Astronomy (Chp 3)
Low Frequency Radio Astronomy
(Chp. 3)
Tools of radio astronomy, Wilson, et
al.

The radio window



The radio window

~15 MHz to ~1.5 THz



The radio window

~15 MHz to ~1.5 THz

Low frequency
cut-off

$$\frac{v_p}{\text{kHz}} = 8.97 \sqrt{\frac{N_e}{\text{cm}^{-3}}}$$

Ionosphere electron
density ?

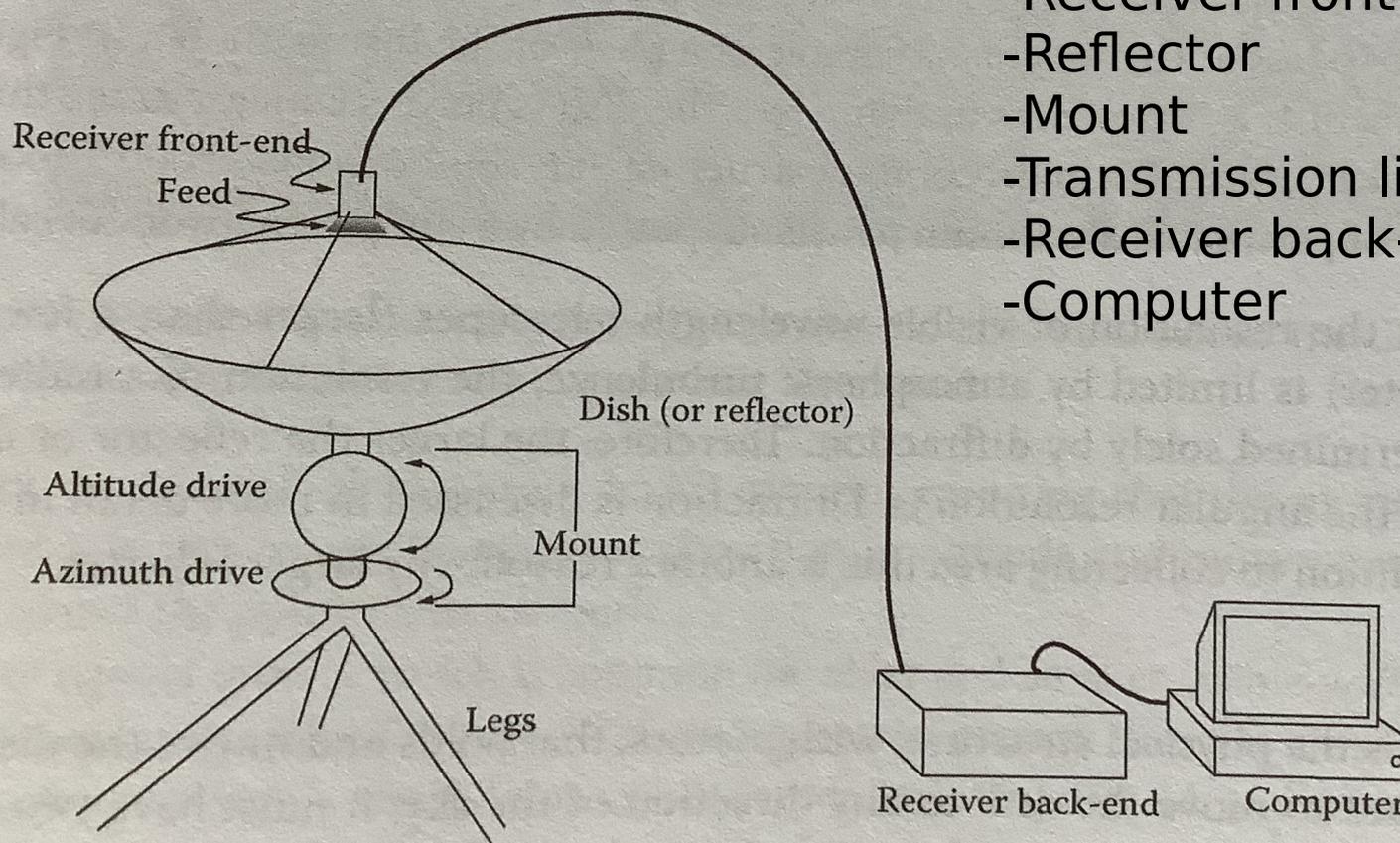
High frequency
cut-off

Water and Oxygen
molecular lines

A basic radio telescope

... (if your school has one), is an example of a prime focus telescope. A color photograph of a Cassegrain telescope is shown in Figure 3.4.

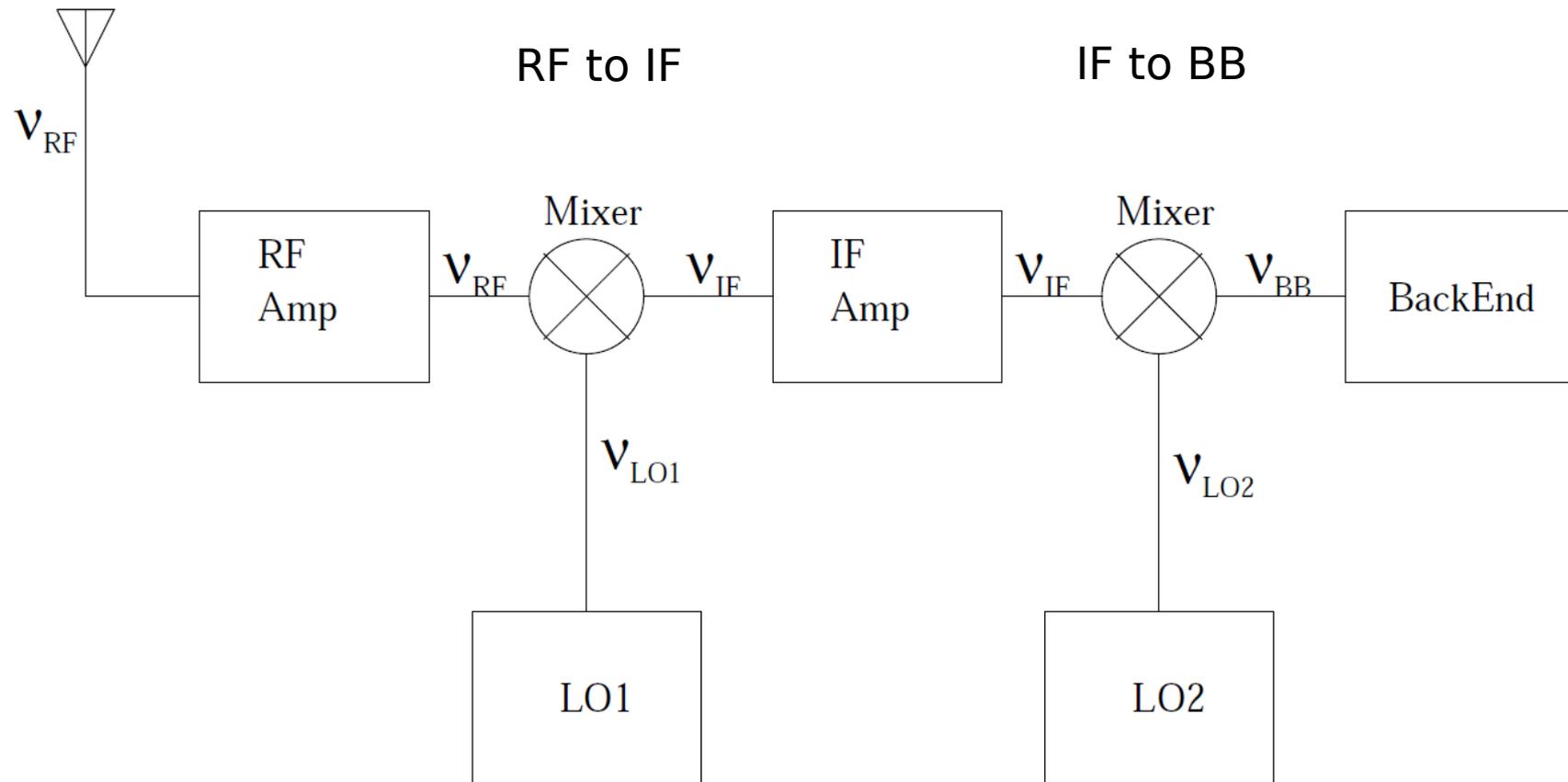
- Feed
- Receiver front end
- Reflector
- Mount
- Transmission lines
- Receiver back-end
- Computer



Radio telescope antennas

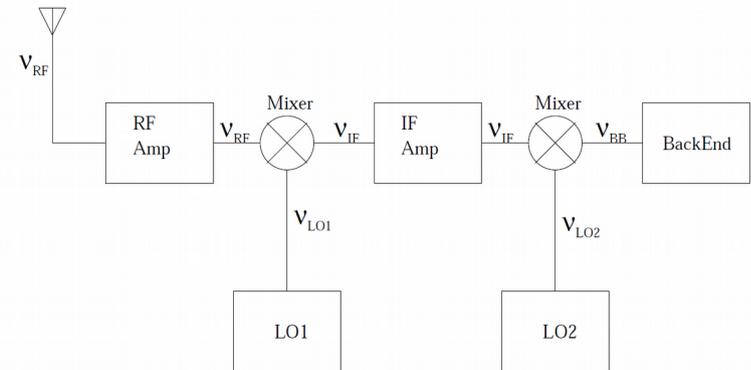
- The region of transition between a free space wave and a guided wave or vice-versa.
- For a radio telescope the antenna acts as a collector of radio waves.
- The response of an antenna as a function of direction is given by the antenna “pattern”. By *reciprocity* this pattern is the same for both receiving and transmitting.

Block diagram of a single dish radio telescope



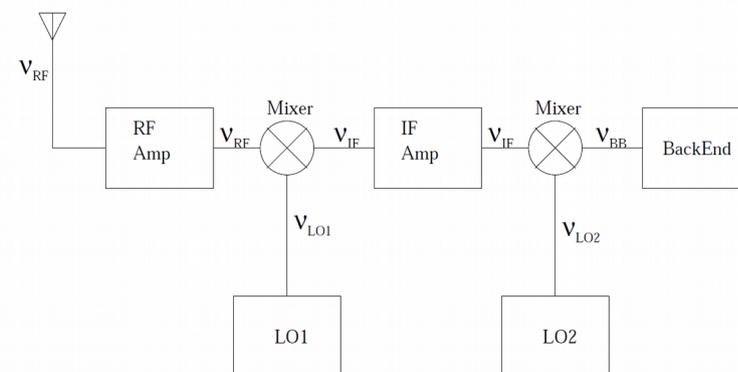
Block diagram of a single dish radio telescope

- EM waves impinge on the antenna and create a fluctuating voltage - frequency is the same as of the incoming wave called *Radio frequency (RF)*.
- Needs *amplification*: Low noise amplifier (LNA) at the receiver front-end amplifies the signal.
- *Mixer*: changes the frequency of the incoming signal. Pure sine wave by tunable signal generator - Local oscillator (LO). Mixing - also called heterodyning.



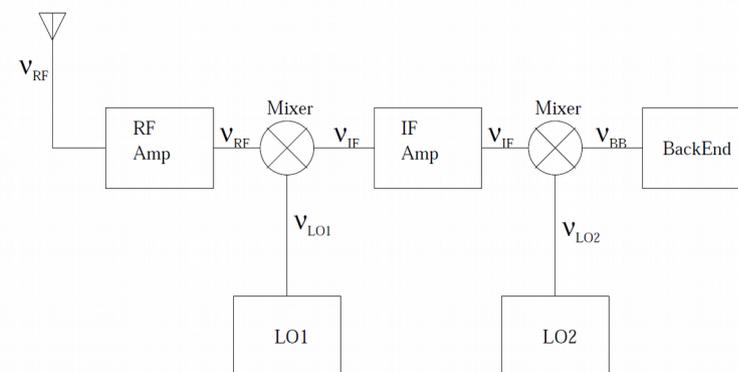
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- Another stage of amplification followed by a mixer to convert the signal to *Baseband (BB)*.
- Passed to a backend: square-law detector/ correlation/ a pulsar backend

Effective aperture

Antenna's ability to absorb the waves that are incident on it is measured by the quantity "effective aperture", A_e .

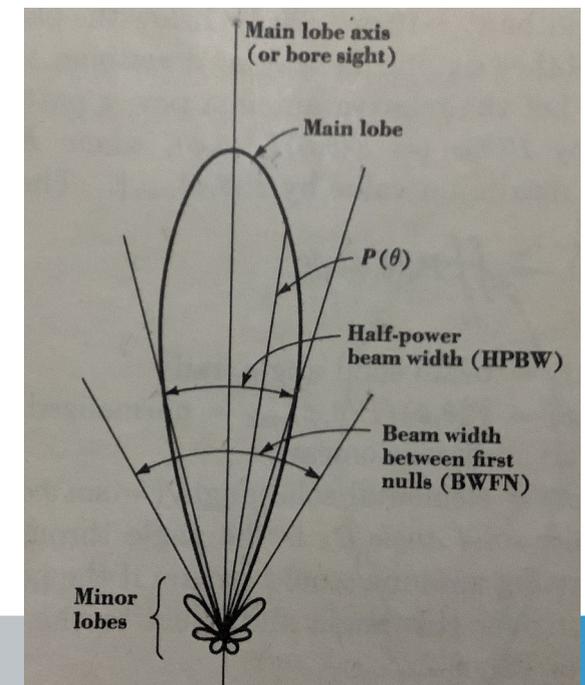
$$A_e = \frac{\text{Power density available at the antenna terminals}}{\text{Flux density of the wave incident on the antenna}} \quad \frac{W/Hz}{W/m^2/Hz} = m^2$$

Also called effective area of the antenna. It is a function of direction, thus:

$$A_e = A_e(\theta, \phi)$$

The power pattern of the antenna describes the directional response of an antenna (normalized to unity at the maximum):

$$P(\theta, \phi) = \frac{A_e(\theta, \phi)}{A_e^{max}} \quad \Theta_{HPBW} \sim \lambda/D$$



Directivity, gain and aperture efficiency

Another measure of the response of the antenna as a function of direction is described by “directivity”:

$$\begin{aligned} D(\theta, \phi) &= \frac{\text{Power emitted into } (\theta, \phi)}{(\text{Total power emitted})/4\pi} \\ &= \frac{4\pi P(\theta, \phi)}{\int P(\theta, \phi) d\Omega} \end{aligned}$$

Aperture efficiency is the ratio of the maximum effective aperture and the geometric cross sectional area of the reflector:

$$\eta = \frac{A_e^{max}}{A_g}$$

Gain and directivity

Gain same as directivity but with an efficiency factor,

$$G(\theta, \phi) = \frac{\text{Power emitted into } (\theta, \phi)}{(\text{Total power input})/4\pi} \eta$$

Aperture efficiency,

$$\eta = \frac{A_e^{max}}{A_g}$$

Gain is often given in decibels (dB) which is:

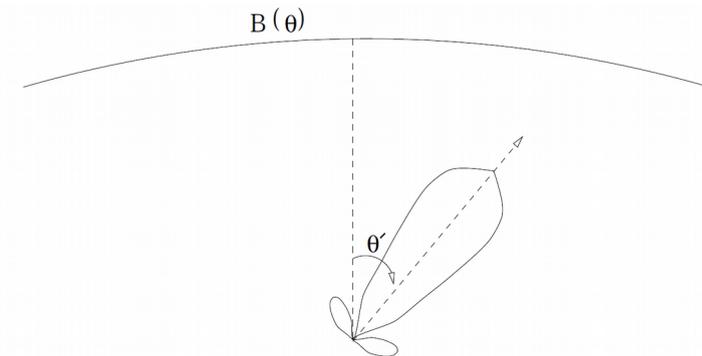
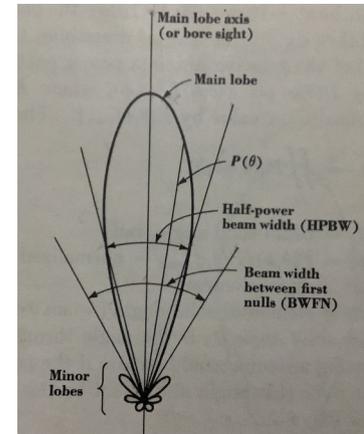
$$G(\text{dB}) = 10 \log_{10} G$$

The convenience is that when there are amplifiers in succession the total gain is simply the addition.

Effect of the pattern on observed sky:

Consider observing a sky brightness distribution $B(\theta)$ with a telescope having a power pattern as shown. Then the power available at the antenna terminals is:

$$W(\theta') = \frac{1}{2} \int B(\theta) A_e(\theta - \theta') d\theta \quad \text{1-dim}$$

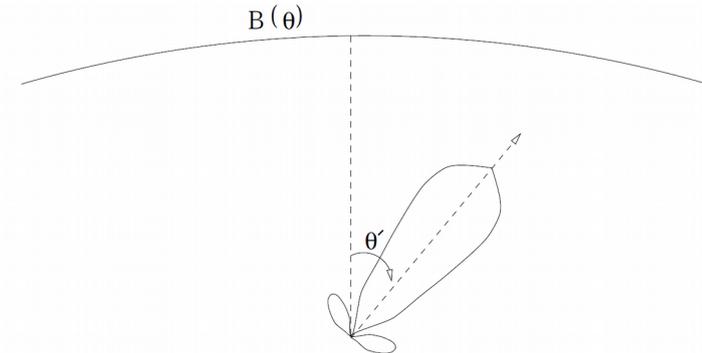
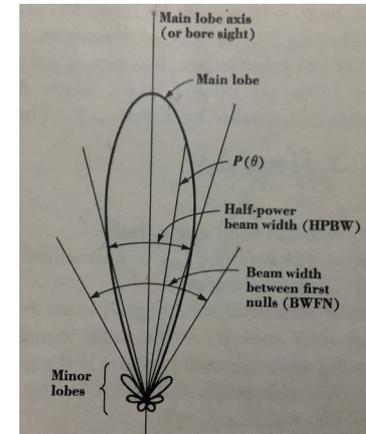


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$\frac{1}{2}$ as only one polarization is absorbed by the antenna



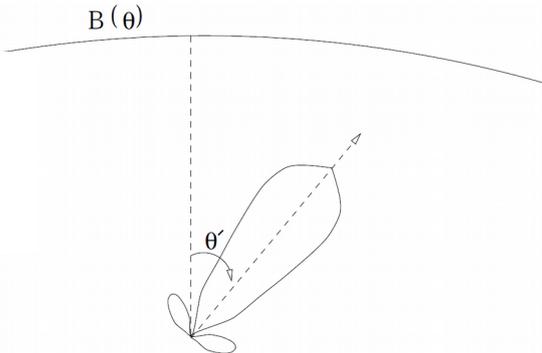
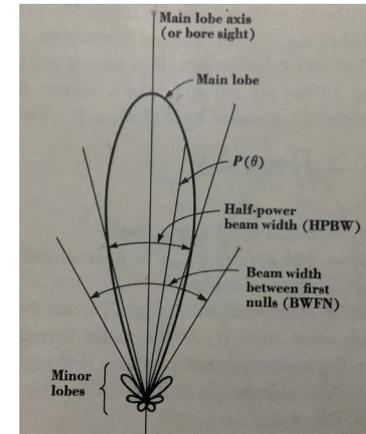
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In 2-dimensions:

$$W(\theta', \phi') = \frac{1}{2} \int B(\theta, \phi) A_e(\theta - \theta', \phi - \phi') \sin(\theta) d\theta d\phi$$



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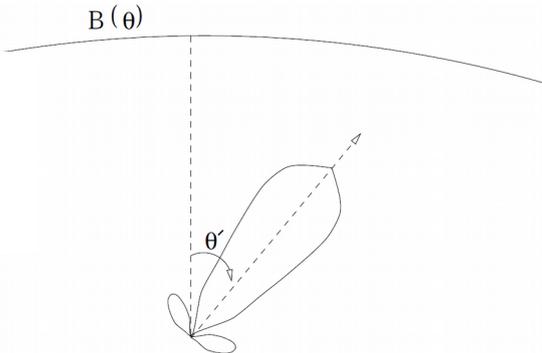
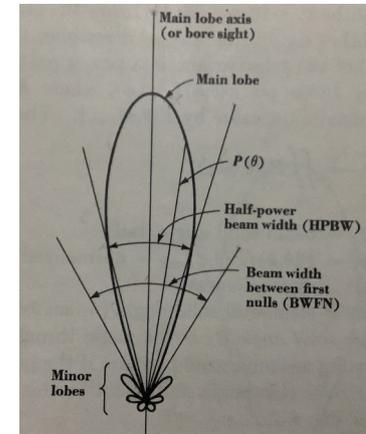
In temperature units,

Recall,

$w = kT$

$$T_B = \left(\frac{\lambda^2}{2k} \right) B(\theta, \phi).$$

$$P(\theta, \phi) = \frac{A_e(\theta, \phi)}{A_e^{max}}$$



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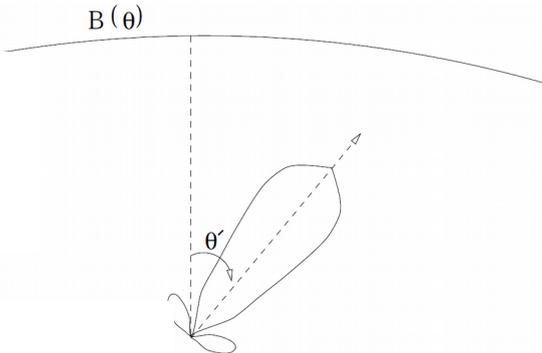
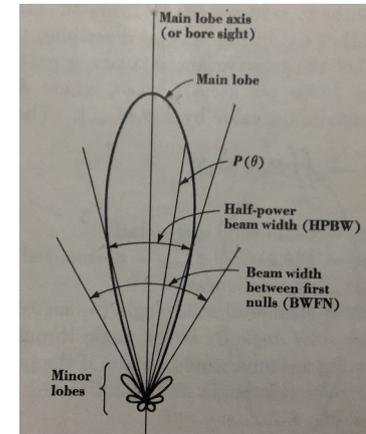
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In temperature units,

$$T_A(\theta', \phi') = \frac{A_e^{max}}{\lambda^2} \int T_B(\theta, \phi) P(\theta - \theta', \phi - \phi') \sin(\theta) d\theta d\phi$$

Antenna temperature is the weighted average of the sky temperature - the weighting function is the power pattern of the antenna.

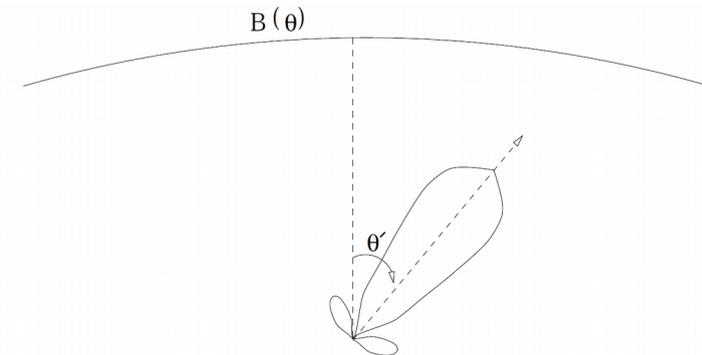
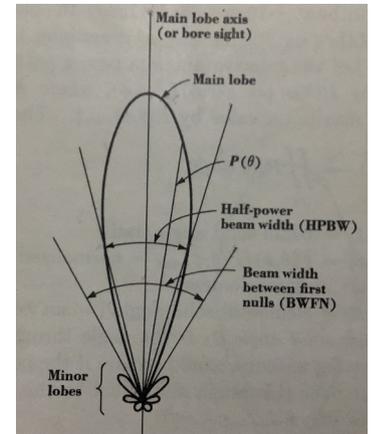


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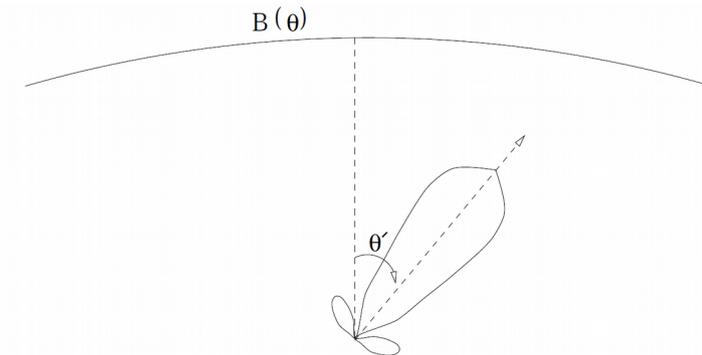
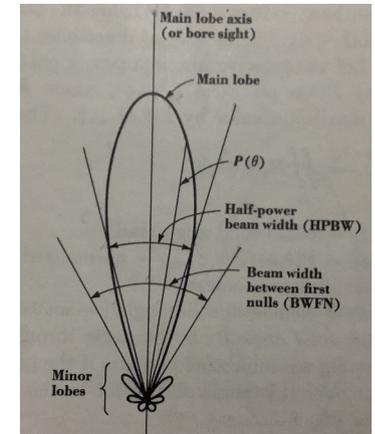
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While scanning the sky, if you observe a rise in antenna temperature, it is unclear if it is due to a single bright source or a collection of faint sources - termed as **confusion noise**.



Confusion noise is a function of frequency and the distribution of sources in the sky

Relation between directivity and effective aperture

Consider an antenna terminated in a resistor and the entire setup placed in a blackbox at temperature T . At thermal equilibrium, the power flowing from resistor to antenna is:

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And that flowing from the antenna to the resistor is:

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Maximum effective aperture is determined by the shape of the power pattern alone.

Relation between directivity and effective aperture

For a reflecting telescope,

$$\int P(\theta, \phi) d\Omega \sim \Theta_{HPBW}^2 \sim \left(\frac{\lambda}{D}\right)^2$$

And thus,

$$A_e^{max} \sim D^2 \qquad \text{Recall, } A_e^{max} = \frac{\lambda^2}{\int P(\theta, \phi) d\Omega}$$

The max. effective aperture scales like the geometric area of the reflector. Also,

$$A_e = A_e^{max} P(\theta, \phi) = \frac{\lambda^2 P(\theta, \phi)}{\int P(\theta, \phi) d\Omega}$$

$$D(\theta, \phi) = \frac{4\pi}{\lambda^2} A_e(\theta, \phi) \qquad \text{Recall: } D(\theta, \phi) = \frac{4\pi P(\theta, \phi)}{\int P(\theta, \phi) d\Omega}$$

Application: Finding power at one antenna from a signal transmitted from another

Consider sending information from antenna 1 with gain $G_1(\theta, \phi)$ and input power P_1 to antenna 2 with directivity $D_2(\theta, \phi)$ at a distance R away.

The flux density at antenna 2 is:

$$S = \frac{P_1}{4\pi R^2} G_1(\theta, \phi)$$

Factor G encodes that the power is not isotropically distributed

Power available at antenna 2 is :

$$W = A_{2e} S = \frac{P_1}{4\pi R^2} G_1(\theta, \phi) A_{2e}$$

Recall: $D(\theta, \phi) = \frac{4\pi}{\lambda^2} A_e(\theta, \phi)$

After substituting for the effective aperture,

$$W = \left(\frac{\lambda}{4\pi R}\right)^2 P_1 G_1(\theta, \phi) D_2(\theta', \phi')$$

Friis transmission equation

Reflector antennas

The most common reflector shape is a paraboloid.

The reflector must keep all parts of an on-axis plane wavefront in phase at its focal point.