Astronomical Techniques I Lecture 10

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For discrete number statistics use Poisson, for continuous number statistics or where mean > 30 use Gaussian.

If u = f(x, y) is a function of two random variables, x and y, then we can propagate the uncertainty in x and y to u as follows:

$$\sigma_{u}^{2} = \sigma_{x}^{2} \left(\frac{\partial u}{\partial x}\right)^{2} + \sigma_{y}^{2} \left(\frac{\partial u}{\partial y}\right)^{2} + 2\sigma_{xy}^{2} \left(\frac{\partial u}{\partial x}\right) \left(\frac{\partial u}{\partial y}\right)$$

where the *covariance* of x and y is defined as

$$\sigma_{xy}^2 = \frac{1}{M} \sum_{i=1}^{M} [(x - \bar{x})(y - \bar{y})]$$

if x and y are independent variables the $\sigma_{xy} = 0$

$$Var(kx) = k^{2} Var(x)$$
$$Var(x + y) = Var(x) + Var(y) + 2\sigma_{xy}^{2}$$
$$Var(xy) = y^{2} Var(x) + x^{2} Var(y) + 2xy\sigma_{xy}^{2}$$

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An Introduction to Error Analysis by John Taylor

Image: A matched a matc

Signal to noise ratio

In crude terms signal to noise ratio is the ratio of the quantity we are interested in to all the quantities we are not interested in, one person's signal is another person's noise.



Definition of S/N ratio

$$\frac{S}{N} = \frac{\bar{x}}{s_{\bar{x}}}$$

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$$\frac{S}{N} = \frac{N_*}{\sqrt{N_* + n_{\text{pix}}(N_S + N_D + N_R^2)}}$$

Why is read noise squared in the above equation?

Three regimes possible

- Source noise dominates
- background noise dominates
- read noise dominates

For bright sources, $N_* >> n_{\rm pix}(N_S + N_D + N_R^2)$ so,

$$rac{S}{N} = rac{N_*}{\sqrt{N_*}} = \sqrt{N_*}$$

This condition is a good definition of a bright source!

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For faint sources, $N_* \sim n_{\rm pix} N_S$ so,

$$\frac{S}{N} = \frac{N_*}{\sqrt{2n_{\rm pix}N_S}}$$

Why does background variance appear twice? How to improve S/N?

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When read noise dominates

 happens when source is faint and background is low. Solution: increase exposure time



One can write $N_* = n_*t$ and $N_S = n_S t$ and $N_D = n_D t$. In source and background dominated regimes $\frac{S}{N} \propto \sqrt{t}$

SNR measures how well an object is detected and characterized.

- S/N = 2 3: object barely detected
- S/N = 5: object detected, can start to believe what one sees
- S/N = 10: can start to do quantitative measurements
- S/N = 100: excellent measurements.

As N (noise) is the error on the measurement, 1 / (S/N) is the relative error on the measurement:

- *S*/*N* = 100: measurement at 1% (0.01 mag)
- *S*/*N* = 10: measurement at 10% (0.1 mag)
- *S*/*N* = 5 : measurement at 20% (0.2 mag)

$$\sigma_{\text{magnitudes}} = \frac{1.0857\sqrt{N_* + n_{\text{pix}}(N_S + N_D + N_R^2)}}{N_*}$$

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Exposure time calculator for IFOSC and sky background estimation

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To correct for the extinction in Earth's atmosphere, we must make observations on nights that are perfectly clear and that have no changes in the basic atmospheric conditions, such as humidity or atmospheric pressure, during the the night.

- Rayleigh scattering
- aerosol scattering
- molecular absorption ("telluric bands") by oxygen, ozone (in UV) and water (in IR).

Earths atmosphere can be approximated as a flat slab of air. That is, initially we ignore the curvature of the atmosphere.

With the atmosphere being treated as a flat slab, we can relate the length of any path through the atmosphere to the minimum distance, which is the path straight up toward the zenith. If we call the minimum path *Z*, any other path length, *L* is given by $L = Z/\cos z = Z \sec z$, where *z* is the zenith angle. The minimum path Z is called 1 Air Mass. The quantity sec *z* gives the actual path through the atmosphere in units of Air Mass. But real atmosphere is *curved*.

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Consider a thin layer of the atmosphere, *dl*. Because of the extinction that takes place in that layer, the light is diminished going through it. This can be written

$$df = -fkdl$$

where f is the flux of light at the top of the layer, and k is the extinction in the layer.

$$df/f = -kdl$$

Integrating

$$ln(f_g/f_0) = -kL \Rightarrow f_0/f_g = e^{kL}$$

$$mag_g - mag_0 = 2.5 \log_{10}(f_0/f_g) = 2.5kL \log_{10} e$$

Defining $k' = 2.5k \log_{10} e$ and using $L = \sec z$

$$mag_g = k' \sec z + mag_0$$

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What real life experience tells you this?

- k' must be determined separately for each filter
- $k' \propto 1/\lambda$ use this if extinction is not available in all filters.

Dust Extinction Service based on Schlegel, Finkbeiner & Davis 1998. http://irsa.ipac.caltech.edu/applications/DUST/

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Ideal versus real filter



The color term



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- PSF/Galaxy profile photometry
- aperture photometry

Crowded field photometry



Aperture photometry



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Aperture photometry and sky estimation



 $m = -2.5 \times \log_{10}(\text{DN} / \text{EXPTIME}) + \text{ZEROPOINT}$

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 $m = -2.5 \times \log_{10}(DN / EXPTIME) + ZEROPOINT + colorterm$

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 $m = -2.5 \times \log_{10}(\text{DN} / \text{EXPTIME}) + \text{ZEROPOINT} + \text{colorterm} + \text{extinction}$

 $m = -2.5 \times \log_{10}(DN / EXPTIME) + ZEROPOINT + colorterm + extinction + galactic extinction$

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 $m = -2.5 \times \log_{10}(DN / EXPTIME) + ZEROPOINT + colorterm + extinction + galactic extinction + K correction$

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 $m = -2.5 \times \log_{10}(DN / EXPTIME) + ZEROPOINT + colorterm +$ extinction + galactic extinction + K correction + cosmological dimming

 $m = -2.5 \times \log_{10}(DN / EXPTIME) + ZEROPOINT + colorterm +$ extinction + galactic extinction + K correction + cosmological dimming + intrinsic dust correction

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 $m = -2.5 \times \log_{10}(DN / EXPTIME) + ZEROPOINT + colorterm +$ extinction + galactic extinction + K correction + cosmological dimming + intrinsic dust correction + intergalactic attenuation

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 $m = -2.5 \times \log_{10}(DN / EXPTIME) + ZEROPOINT + colorterm +$ extinction + galactic extinction + K correction + cosmological dimming + intrinsic dust correction + intergalactic attenuation + aperture correction

 $m = -2.5 \times \log_{10}(DN / EXPTIME) + ZEROPOINT + colorterm +$ extinction + galactic extinction + K correction + cosmological dimming + intrinsic dust correction + intergalactic attenuation + aperture correction + bad pixel correction

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Astronomical photometry by Henden & Kaitchuk Introduction to astronomical photometry by Budding & Demircan