Astronomical Techniques II Lecture 2 - Single Dish Astronomy

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March-May 2016

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Brightness

Assumption

- No absorption, emission, scattering or any other propagation effect along the path, or propagation through empty space
- Geometric optics

Brightness - $B(\theta, \phi, \nu, t)$

- Units $W m^{-2} sr^{-1} Hz^{-1}$
- AKA Surface Brightness, Specific Intensity or Spectral Radiance
- Conserved along a ray in empty space

Power received at a detector

$$dW = B(heta, \phi,
u) \ cos heta dA \ d\Omega \ d
u$$

 dW - W
 $B(heta, \phi) - W \ m^{-2} \ sr^{-1} \ Hz^{-1}$

Practical quantitative definition

$$B(\theta, \phi, \nu) = \frac{dW}{d\Omega \cos\theta dA \ d\nu}$$

- Intrinsic property of the source
- Independent of the distance from the source (ONLY for a resolved object)
- Can be thought of as energy *received* at the detector OR as energy *emitted* by the source.

Total Intensity - Specific Intensity integrated over frequency Conservation of Brightness applies here as well Example: Looking through a telescope

Flux Density, S_{ν}

 Total spectral power received from a source by a detector of unit area.

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$$S_{\nu} = \int_{Source} B(\theta, \phi, \nu) \cos\theta \ d\Omega$$

For a source with a well defined solid angle

• Unit -
$$W m^{-2} Hz^{-1}$$

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• 1 Jansky
$$(Jy) = 10^{-26} W m^{-2} Hz^{-1}$$

Flux Density, S_{ν}

 Not an intrinsic property of the source - dependent on the distance to the source

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- The $cos\theta$ is ~ 1.0 if angular size << 1 rad
- Useful for compact (unresolved) sources

Luminosity

Spectral Luminosity

- \blacksquare Total power radiated by the source per unit bandwidth at ν
- $L_{\nu} = 4\pi \ d^2 \ S_{\nu}$
- Property of the source
- Involves *d*, the distance to the source!

Bolometric Luminosity

Total power radiated by the source integrated over the entire spectrum

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$$L_{bol} = \int_0^\infty L_\nu \ d\nu$$

Assume the Sun to be blackbody at 5800 K. What is the specific intensity of the Sun at $\nu = 10 GHz$? What is the flux density of the Sun measured at Earth

- 1 Verify if Rayleigh Jeans law is applicable
- **2** Use it to compute B_{ν}
- **3** To get S_{ν} , compute the angular size of the Sun. Assume the Sun to be a disc of uniform *Brightness* and integrate over it.

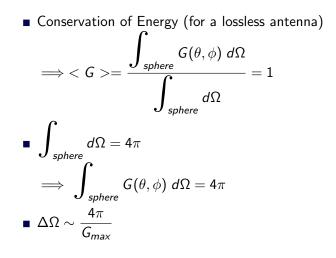
How will B_{ν} and S_{ν} change if they are measured from Mars, rather than the Earth?

Submit your solution in the next class!

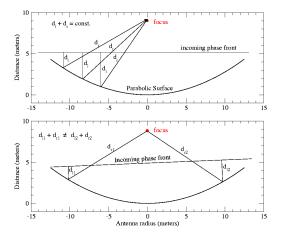
$G(\theta, \phi) = Power \text{ transmitted towards } (\theta, \phi) \text{ (per unit solid angle)}$ Power transmitted by an isotropic antenna (per unit solid angle)

- Dimensionless
- Measure of how directional an antenna is
 - Gain of an isotropic antenna is 1.0
- Usually expressed in dB, i.e. $G(dB) = 10 \times log_{10}G$
- For a lossless antenna, same as the *Directivity* as well.

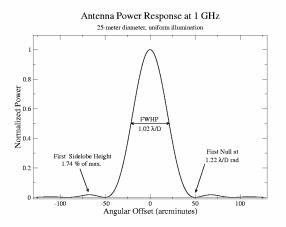
Gain of an Antenna, $G(\theta, \phi)$



Directivity of a Parabolic Dish

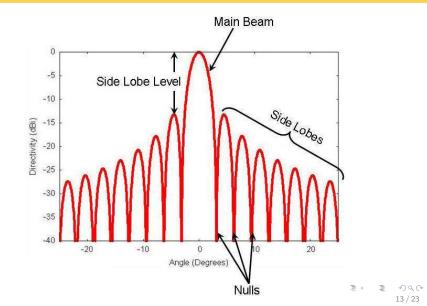


Directivity of a Parabolic Dish



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Directivity of a Parabolic Dish



A Measured Antenna Pattern (ATA)

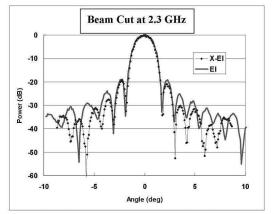
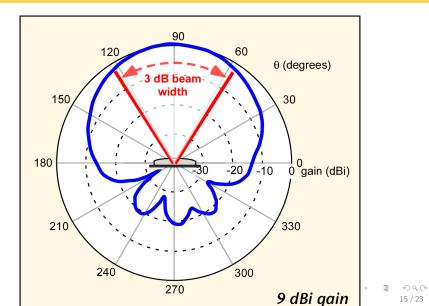


Figure 1: Two cuts through the primary beam pattern of one of the ATA dishes.

Antenna Pattern of a Patch Antenna



Beam shape of Arecibo Antenna

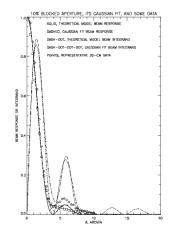


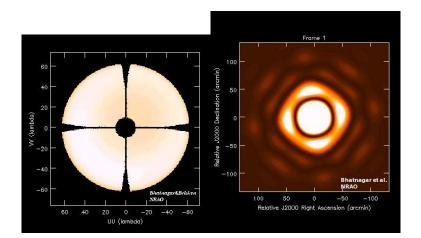
Fig. 4.— Normalized power pattern P_{α} , and also the integrand ΦP_{α} for (1) the standard model of a uniformly illuminated 10% blocked aperture (solid, dash-dot lines), and (2) its Gaussian-Bit counterpart (dash, dash-dot-dot-dot lines). The squares and diamonds are representative data points for P_{α} from the LBW feed at 1415 MHz, obtained by averaging different cuts in one single observing pattern.

 $E(\psi, \eta)$ - Aperture illumination (electric field distribution across the aperture) ψ and η - aperture coordinates

 $U(\alpha, \beta)$ - Far field electric field (diffraction pattern) α and β - directions relative to the optical axis of the telescope

 $E(\psi,\eta)$ and U(lpha,eta) form a Fourier transform pair

An Example (Model for VLA 1420 MHz)



Normalised Antenna Power Pattern, $P(\theta, \phi, \nu)$

$$P(\theta, \phi, \nu) = \frac{G(\theta, \phi, \nu)}{G(\theta_0, \phi_0, \nu)}$$

where θ_0 and ϕ_0 define the optical axis of the aperture.

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$$\int_{sphere} P(\theta, \phi, \nu) \ d\Omega = \Omega_A$$
$$\Omega_A - \text{Beam solid angle}$$
•
$$\lambda^2 = \Omega_A \times A_{eff}$$

• For an isotropic antenna $A_{eff} = \frac{\lambda^2}{4\pi}$

Gain and Aperture

$$G = rac{A_{eff}}{\lambda^2/4\pi}, \; A_{eff} - \; {
m Effective \; collecting \; area}$$

 $A_{eff} = \eta \; A_{geom}$

- η typically in the range 0.35 0.7
- GMRT: $\eta \sim$ 0.65–0.60 in the range 150 610 MHz, and \sim 0.4 at 1400 MHz.
- J-VLA: η peaks at 3 GHz at ~0.62, and drops to ~0.45 at 1.4 GHz and ~0.34 at 45 GHz
- ALMA: $\eta \sim$ 0.75–0.45 in the range 35 850 GHz

Spectral Power

$$W = \int_{\nu} \int_{aperture} \int_{\Omega} B(\theta, \phi, \nu) \cos\theta dA \ d\Omega \ d\nu \quad W$$

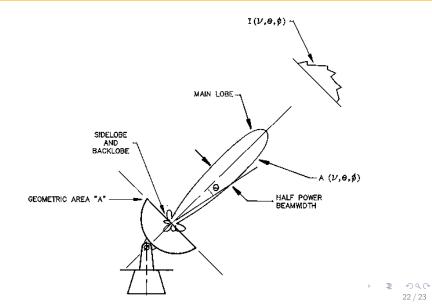
$$w_{
u} = \int_{aperture} \int_{\Omega} B(\theta, \phi, \nu) \cos \theta dA \ d\Omega \ W \ Hz^{-1}$$

$$w_{
u} = A_{eff} \int_{\Omega} B(\theta, \phi, \nu) \cos \theta \ d\Omega \ W \ Hz^{-1}$$

$$w_{
u} = A_{eff} \int_{\Omega} B(heta, \phi,
u) \ P(heta, \phi,
u) \ d\Omega \ W \ Hz^{-1}$$

For a uniform source of Brightness B_u , this becomes $w_{\nu} = \frac{1}{2} A_{eff} B_u \Omega_A \quad W Hz^{-1}$

The image to keep in mind



- References:
 - Kraus Radio Astronomy (2nd ed): Sec 3.1–3.5
- Pre-requisites:
 - Concepts of blackbody radiation, Planck's law, Rayleigh-Jeans law
 - Concepts of random variables and statistics